

# Perth College

### Semester Two Examination, 2017

### Question/Answer booklet

# YEAR 11

If required by your examination administrator, please place your student identification label in this box

# MATHEMATICS

**METHODS**

**UNITS 1 AND 2**

## Section Two:

## Calculator-assumed

|  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Student Number: In figures |  |  |  |  |  |  |  |  |  |  |

In words

Your name

## Time allowed for this section

Reading time before commencing work: ten minutes

Working time: one hundred minutes

## Materials required/recommended for this section

***To be provided by the supervisor***

This Question/Answer booklet

Formula sheet (retained from Section One)

***To be provided by the candidate***

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

## Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

## Structure of this paper

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Working  time (minutes) | Marks available | Percentage of examination |
| Section One:  Calculator-free | 8 | 8 | 50 | 52 | 35 |
| Section Two:  Calculator-assumed | 13 | 13 | 100 | 98 | 65 |
|  | | |  | **Total** | 100 |

## Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.

2. Write your answers in this Question/Answer booklet.

3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.

4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.

5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.

6. It is recommended that you do not use pencil, except in diagrams.

7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section Two: Calculator-assumed 65% (98 Marks)

This section has**thirteen (****13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 9 (6 marks)

(a) The tangent to the curve at intersects the -axis at . Determine the value of . (3 marks)

(b) If and , determine . (3 marks)

Question 10 (8 marks)

A group of 240 students were asked whether they had bought a drink or a snack from the school canteen. 72 had bought neither, 128 had bought a snack and 48 had bought both.

(a) Determine the number of students who only bought a drink. (2 marks)

(b) Determine the probability that a randomly chosen student from the group had bought

(i) a snack or a drink. (1 mark)

(ii) only a snack. (1 mark)

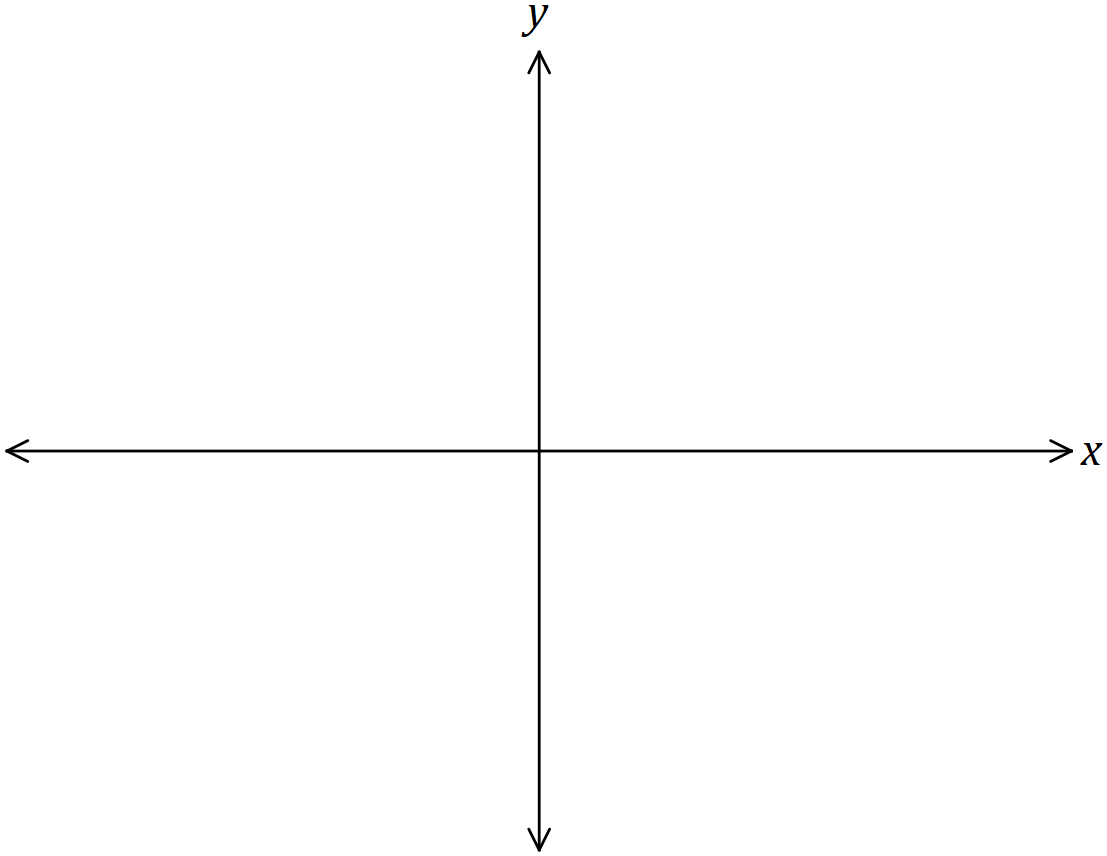
(iii) a snack given that they had bought a drink. (2 marks)

(c) For this group of students, are the events buying a snack and buying a drink independent? Justify your answer. (2 marks)

Question 11 (6 marks)

Line has equation .

(a) Sketch the graph of , showing all intercepts. (2 marks)

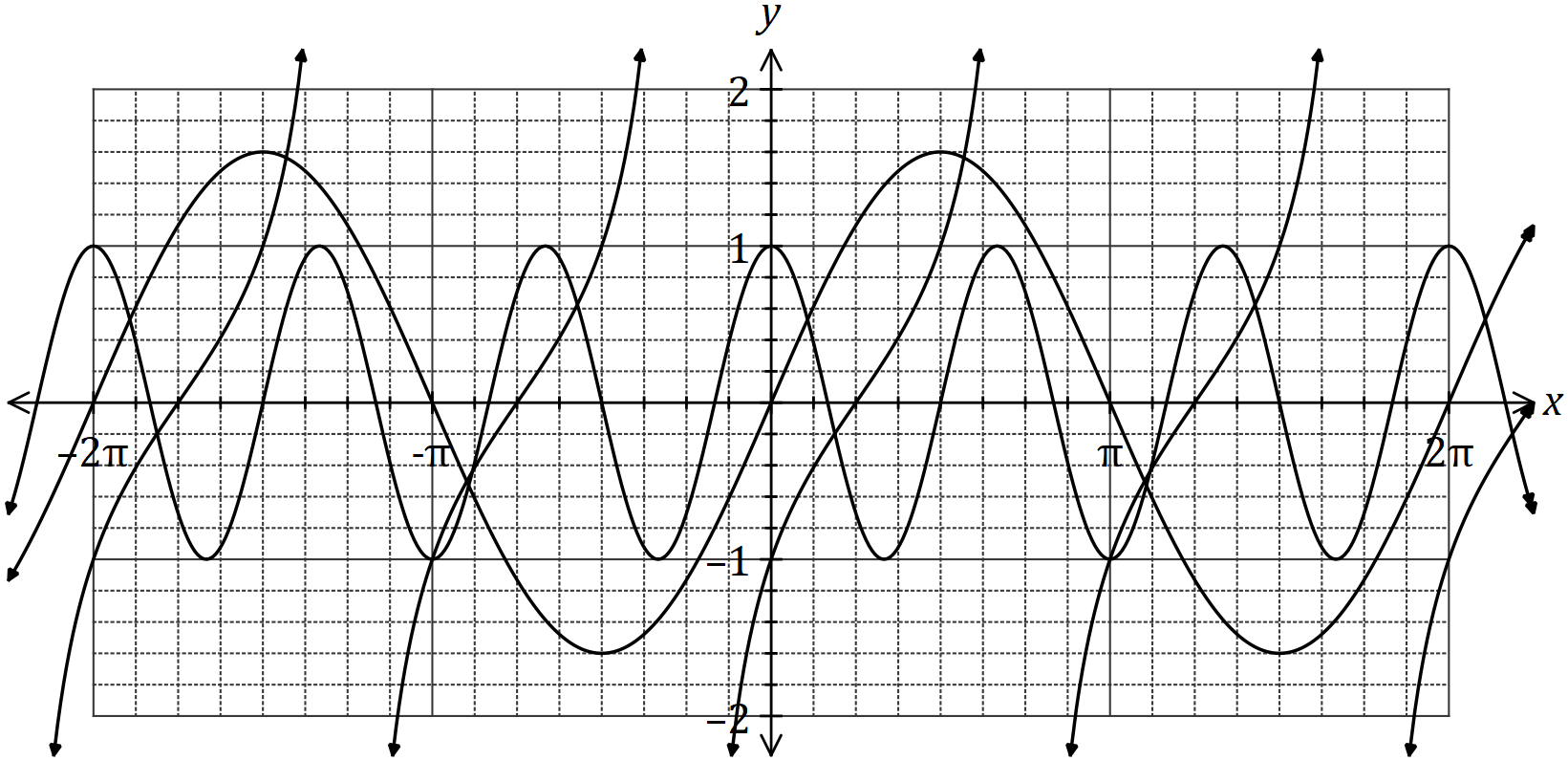


(b) Determine the equation of line that is parallel to and passes through the point with coordinates . (2 marks)

(c) Determine the equation of line that is perpendicular to and has the same -intercept as . (2 marks)

Question 12 (7 marks)

(a) The graphs of , and are shown below.



Determine the values of the constants , and . (3 marks)

(b) One day, the depth of water in a tidal basin was modelled (in radians) by , where was the depth in metres and was the time, in hours, after midnight. For this day, determine

(i) the depth of water at 4.30 am. (2 marks)

(ii) the first time in the **afternoon** that the depth of water was 7 m. (2 marks)

Question 13 (6 marks)

The quadratic function passes through and has roots at and .

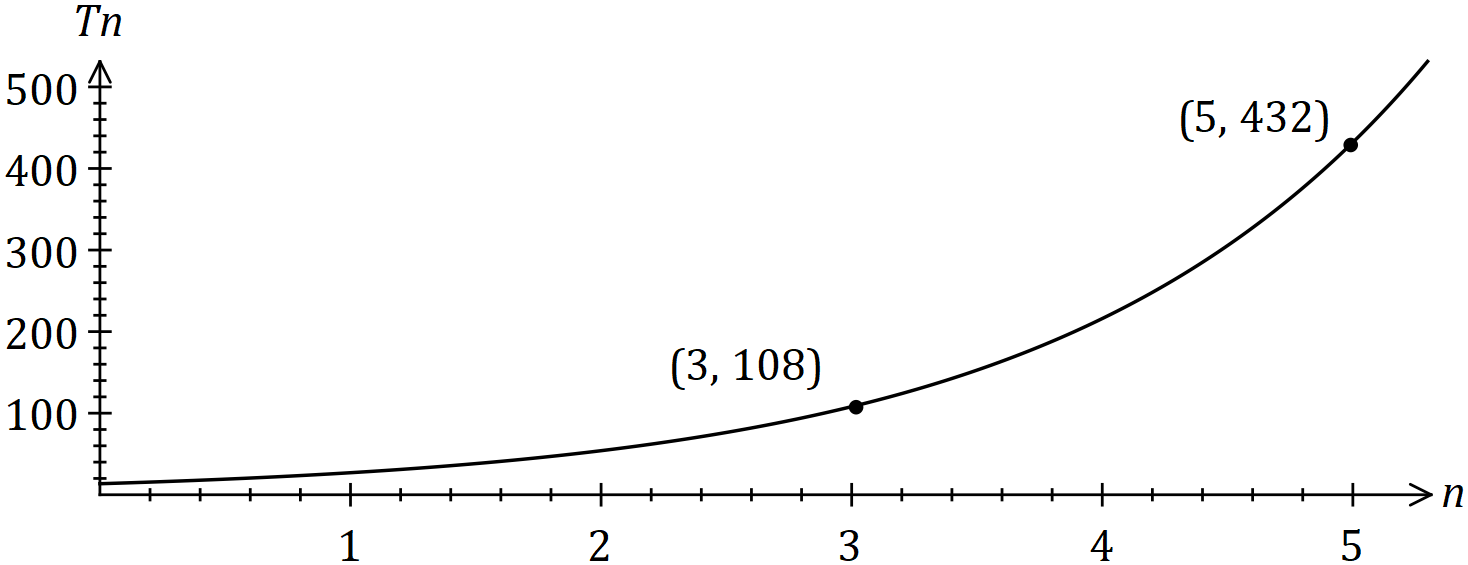
(a) Determine the values of the constants , and . (3 marks)

(b) State the -intercept of the graph . (1 mark)

(c) State the roots of the graph . (2 marks)

Question 14 (8 marks)

The number of followers of a social media influencer, counted at the start of five successive months, is shown in the exponential graph below.



The number of followers () at the start of month can be modelled by the recursive equation .

(a) Use the graph to determine the values of and . (3 marks)

(b) Assuming the growth rate continues,

(i) how many followers are expected at the start of month 12? (1 mark)

(ii) at the start of which month will the number of followers first exceed 750 000?

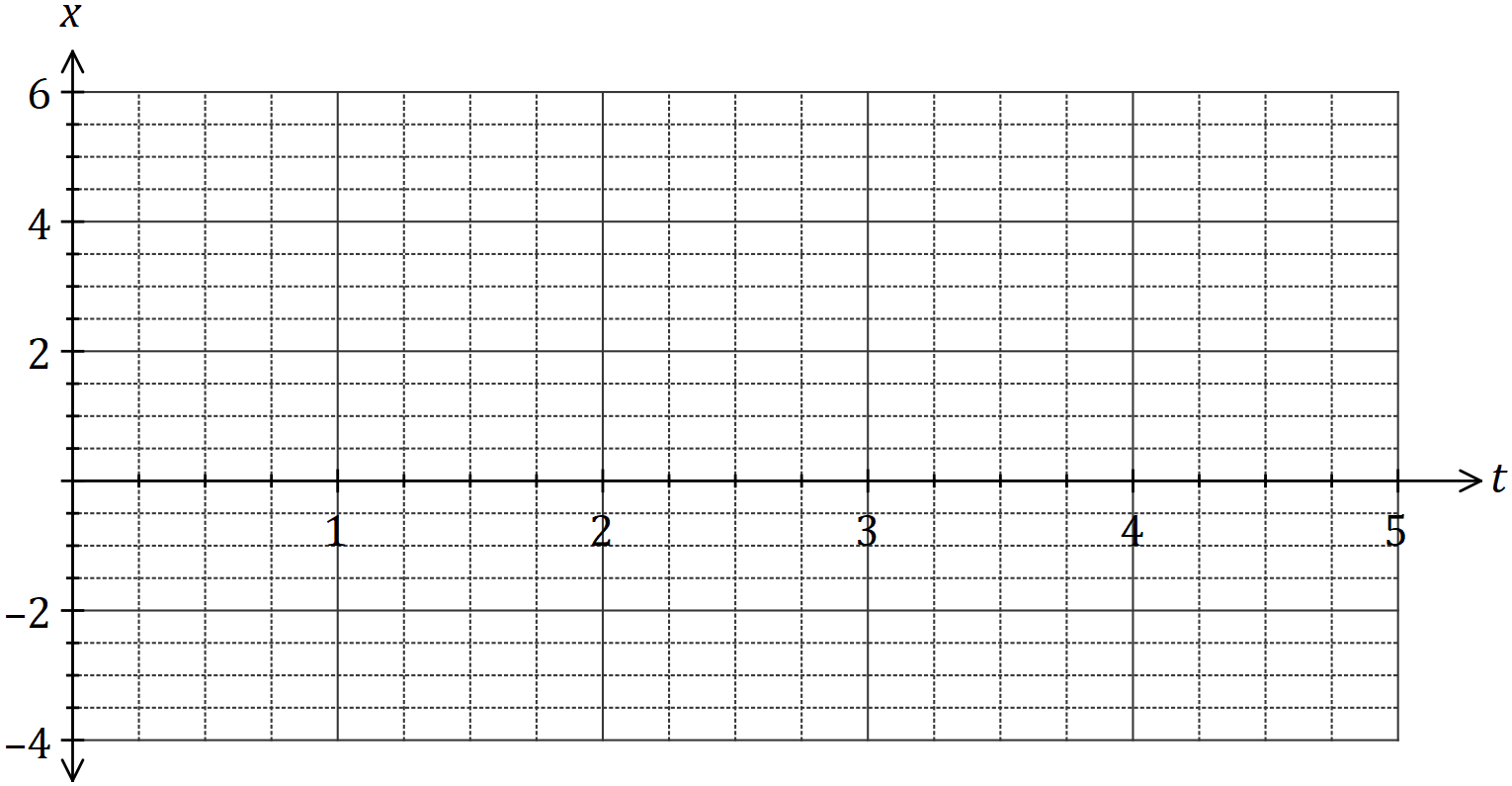
(1 mark)

(c) When the number of followers reached 1 million, the influencer fell out of favour and started to lose 25% of their followers each month. After how many months **from this time** will they have less than 2 000 followers? (3 marks)

Question 15 (8 marks)

A particle is moving along a straight line so that its displacement, metres, from a fixed point after seconds is given by

(a) Sketch the displacement of the particle on the axes below for , labelling key points. (3 marks)



(b) Determine the velocity of the particle when . (2 marks)

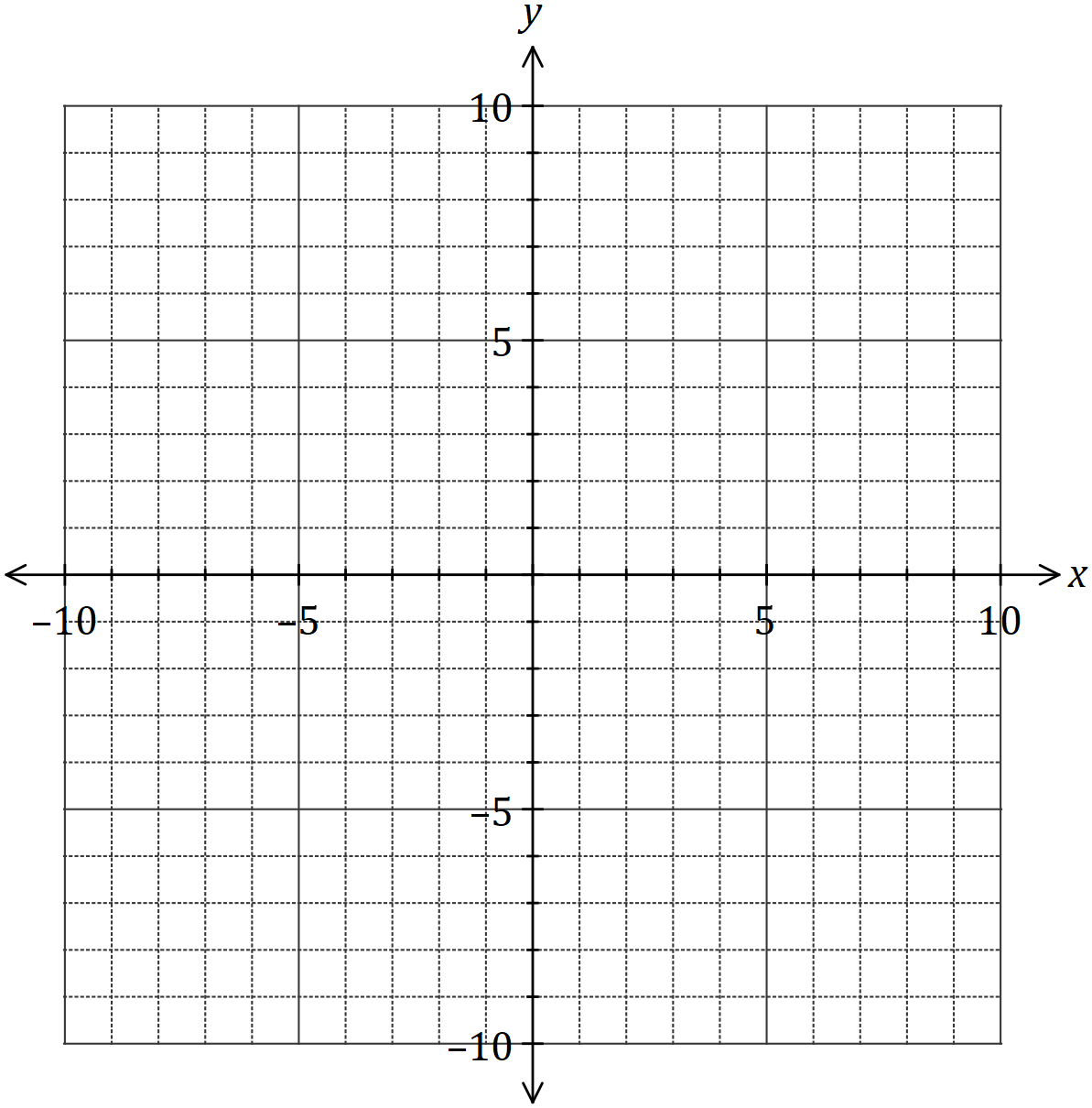
(c) For how long during the first five seconds is the graph decreasing? (1 mark)

(d) Determine the time(s) when the velocity of the particle is -3.6 m/s. (2 marks)

Question 16 (6 marks)

(a) The variables and are related by .

(i) Sketch the graph of this relationship, showing all key features. (3 marks)

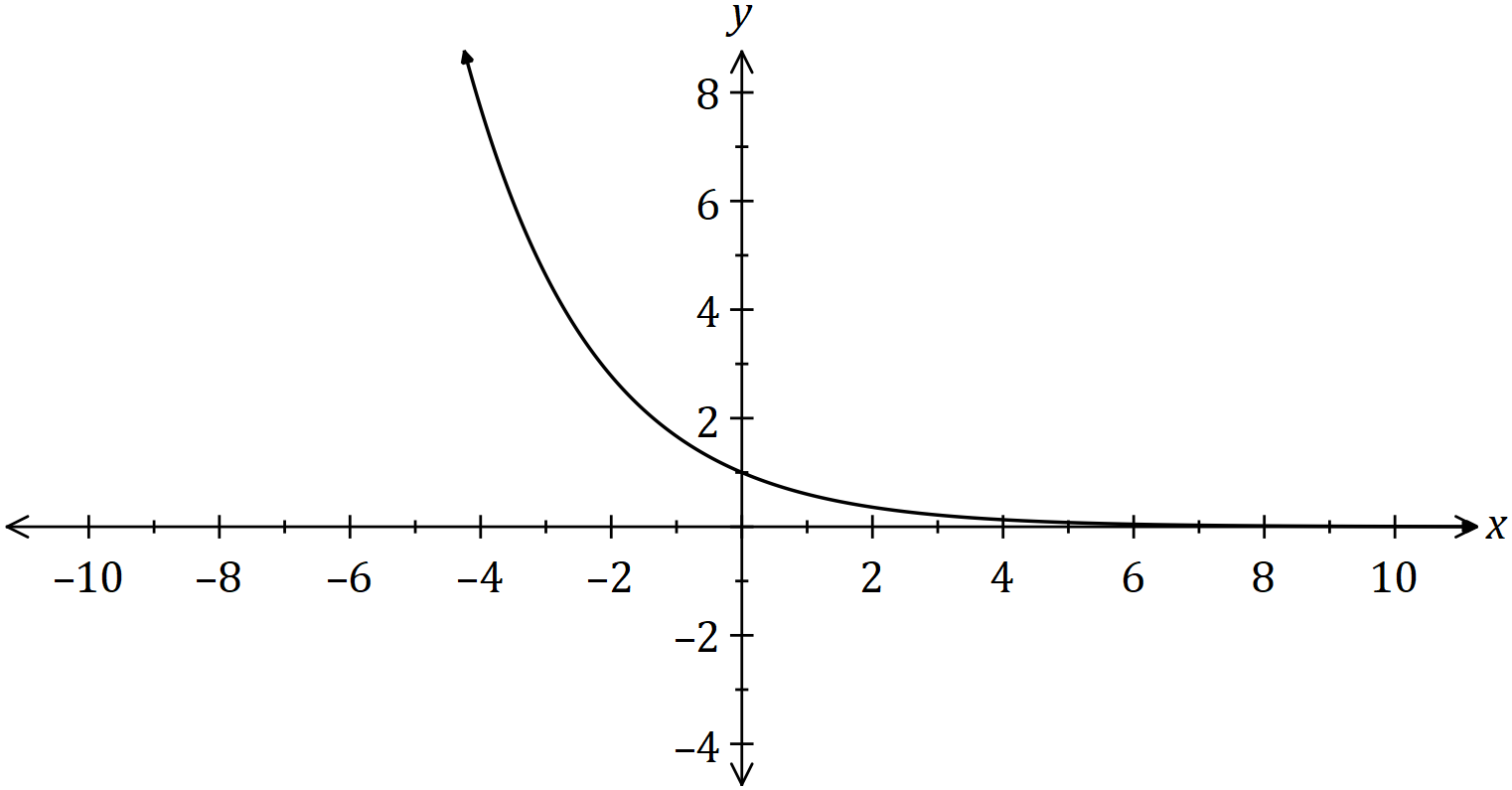


(ii) How does the vertical line test indicate that is not a function of ? (1 mark)

(b) State the domain and range of the function . (2 marks)

Question 17 (8 marks)

The graph of is shown below, where is a positive constant.



(a) On the same axes, sketch and label the graphs of

(i) . (2 marks)

(ii) . (2 marks)

(b) The graph of intersects the graph of when

Determine, giving your answers to 3 significant figures,

(i) the -coordinate of the point of intersection. (1 mark)

(ii) the value of the constant . (HINT: don’t use any previously rounded solution)

(3 marks)

Question 18 (8 marks)

Five different letters are selected from the eleven in the word COMRADESHIP. The order in which the letters are selected is not important, so that the selection COMRA is the same as the selection RAMOC, and so on.

(a) Determine the number of different selections

(i) of five letters. (2 marks)

(ii) of five letters that contain one vowel and four consonants. (2 marks)

(b) Determine the probability that a random selection of five different letters

(i) includes the letters M and R. (2 marks)

(ii) includes at least one vowel. (2 marks)

Question 19 (8 marks)

Events and occur at random and it is known that and .

Determine when

(a) and are mutually exclusive. (1 mark)

(b) . (1 mark)

(c) . (1 mark)

(d) . (2 marks)

(e) and are independent. (3 marks)

Question 20 (11 marks)

Two circles of radii 10 cm and 13 cm have centres at and respectively. The centres are 7 cm apart and the circles intersect at and .

(a) Sketch a diagram of the two circles and clearly show triangle . (2 marks)



(b) Show that , when rounded to one decimal place. (2 marks)

(c) Determine the length of the chord to the nearest millimetre. (2 marks)

(d) (i) Find the obtuse , in radians, correct to three decimal places. (1 mark)

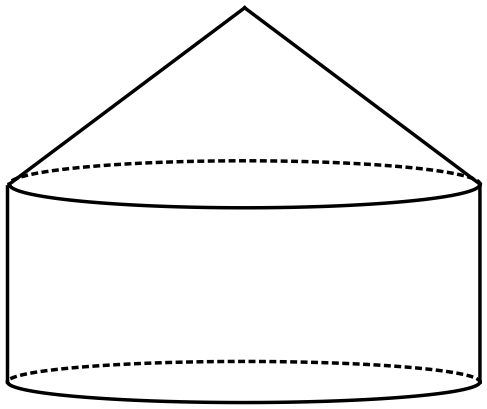
(ii) Find the reflex , in radians, correct to three decimal places. (1 mark)

(iii) Determine the area common to both circles. Answer to one decimal place.

(3 marks)

Question 21 (8 marks)

A composite solid is made from a cone and a cylinder, both of height cm and radius cm, as shown below.



The dimensions are such that the sum of and is cm.

(a) Show that the volume of the solid is given by . (2 marks)

(b) Use calculus techniques to determine the values of and that will maximise the volume of the solid, and state this maximum volume. (6 marks)

Additional working space

Question number: \_\_\_\_\_\_\_\_\_

Additional working space

Question number: \_\_\_\_\_\_\_\_\_

Additional working space

Question number: \_\_\_\_\_\_\_\_\_

|  |  |  |
| --- | --- | --- |
| Markers use only | | |
| Question | Maximum | Mark |
| 9 | 6 |  |
| 10 | 8 |  |
| 11 | 6 |  |
| 12 | 7 |  |
| 13 | 6 |  |
| 14 | 8 |  |
| 15 | 8 |  |
| 16 | 6 |  |
| 17 | 8 |  |
| 18 | 8 |  |
| 19 | 8 |  |
| 20 | 11 |  |
| 21 | 8 |  |
| S2 Total | 98 |  |
| S2 Wt (×0.6633) | 65% |  |